

理数系教員授業力向上研修会(京都)

2018年7月8日(日) 京都テルサ

身近な事象や現象に注目して探究する 「課題研究」の取り組み

広島大学附属中・高等学校
数学科 橋本 三嗣



広島大学

SSH事業と課題研究

平成15年度から指定を受け、継続的に研究開発に取り組んでいる。
平成30年度から新たに第4期目の指定を受けている。

【第4期研究開発課題】

社会に開かれた科学技術を先導する人材育成の起点となる科学教育カリキュラムの開発

【研究仮説】

教育課程上に学校設定教科「SAGAs(探す)」を設置し、「課題研究」を中核とした科学教育カリキュラムを開発、実施することによって、科学的(Scientific)、高度かつ専門的(Academic)、国際的(Global)、主体的・自律的(Autonomous)な素養を備えた「Sagacity((賢明な判断が下せる)洞察力, 深い知性, 先見の明)」を形成し、社会に開かれた科学技術(未来社会の創造に向けた科学技術イノベーション)を先導する人材を育成・輩出することができる。

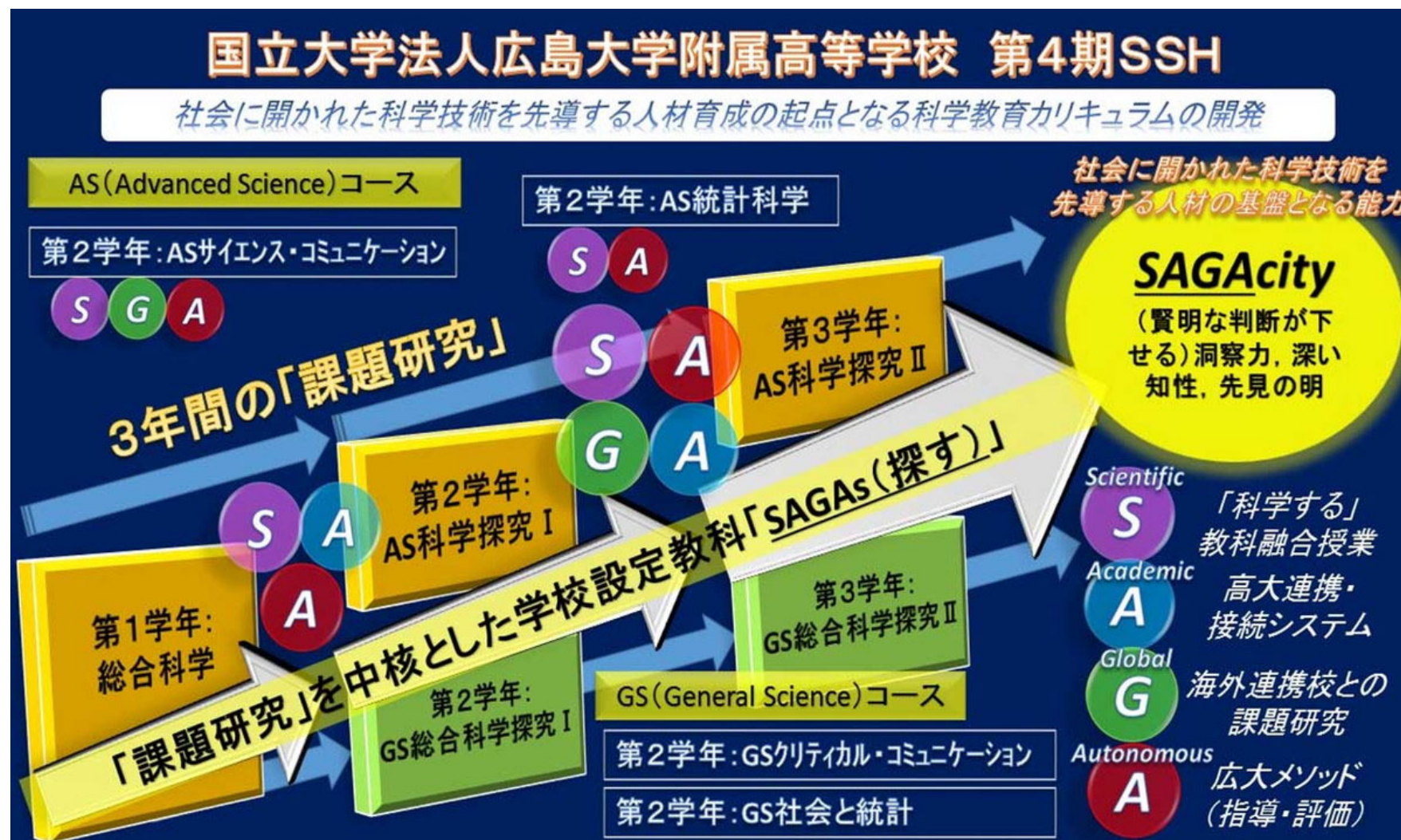
SSH事業と課題研究

【研究開発の目的】

社会的変化が人間の予測を超えて加速度的に進展する大変革時代に、「社会に開かれた科学技術(未来社会の創造に向けた科学技術イノベーション)」を先導する人材を育成、輩出するために、その基盤となる能力「Sagacity」を形成する学校設定教科・科目を教育課程上に設置し、「課題研究」を中核とした科学教育カリキュラムを開発する。

SSH事業と課題研究

【研究開発概念図】



SSH事業と課題研究

【研究開発の内容】



SSH事業と課題研究

【学校設定教科「SAGAs(探す)」】

第2学年より普、通科5クラスのうち、1クラスをAS(Advanced Science)コース、4クラスをGS(General Science)コースとする。

新・学校設定教科「SAGAs(探す)」			第2学年より、普通科5クラスのうち、 1クラスをASコース、4クラスをGSコースとする
	AS(Advanced Science)コース	GS(General Science)コース	SSHの4つの柱
3年	AS科学探究Ⅱ(1単位)	GS総合科学探究Ⅱ(1単位)	
	AS科学探究Ⅰ(2単位)	GS総合科学探究Ⅰ(2単位)	
2年	AS統計科学(1単位)	GS社会と統計(1単位)	
	ASサイエンス・コミュニケーション(1単位)	GSクリティカル・コミュニケーション(1単位)	
1年	総合科学(2単位)		

現高3生の課題研究テーマ

分野	テーマ
物理	「マイクロバブルの効率的発生」 「心柱を科学する」
化学	「泡と洗浄能力の関係」 「アルギン酸樹脂の性質向上」 「シリカゲルの吸着性能について」
生物	「ゼブラフィッシュの嫌悪記憶とその解消について」 「身近なコケを用いた金属イオンの回収」
地学	「広島花崗岩中に見られる包有岩の形状と形成過程」
数学	「蚊柱の数理的モデリング」 「n stroke times～奇点と筆数の関係～」 「コインの行方」

The shape of inclusion in Hiroshima granite

Hiroshima University High School
Oda Kohei Katayama Taro Yamashita Shuhei

Abstract The purpose of this study is to reveal the formation process of dark inclusions. Dark inclusions, which are contained in granites, are classified as a sort of xenolith. According to the research in Motoujina, they seemed to be ellipsoid. And the data on their numerical flatness shows that it falls within a certain value range. Judging from both mathematical inspection and the value, the shapes of dark inclusions are almost determined.

Background

- (1) **Hiroshima granite**: Distributed in the south of Chugoku mountainous district, especially around Hiroshima city¹⁾
- (2) **Dark Inclusion(DI)**:
 - Mafic (including Mg and Fe)
 - Dark mineral
 - Seen in the granites
 - Smaller grain²⁾
 → Its origin ... **Not well known**
- (3) Previous study:
 - Tainosho(1984)³⁾ ... Conducting chemical analysis to reveal what chemicals compose DI
 - Oshima et al.,(2016)⁴⁾ ... Finding DI in Ninoshima, Hiroshima, but its origin not solved



Fig.1 Dark Inclusions (The arrow points to DI.)

Purpose To Reveal how DI was formed

Hypothesis Shape: Ellipsoid

Field Study In order to make clear the shape of DI

- Place: Motoujina ... Tied island connecting to Hiroshima
- Exposed Hiroshima granite, and rich in DI
- Way: Look for DI in outcrop → calculate flatness value



Fig.2 Location of Motoujina



Fig.3 Flatness Value (Schema)

Result Histogram of Flatness Value (Fig.4)

Consideration

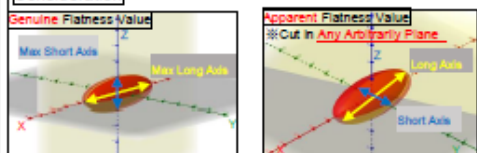


Fig.6 Flatness value in ellipsoid

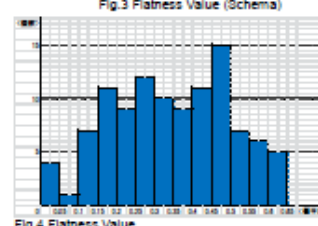


Fig.4 Flatness Value

Conclusion Shape of DI approaches to ellipsoid.

Prospect We are going to focus on the relation between DI and magma

- Conducting model experiment to examine direction of DI in magma
- Investigating geological features of Motoujina in detail, and comparing the distribution of DI

Reference

- 1) 堀本幸男ほか(1987), 日本の地質 7 中国地方, 共立出版
- 2) 堀本幸男ほか(2012), フィールドジョーロジ-8 火成作用, 共立出版
- 3) 田嶋庄良(1984), 「英米複合花崗岩体の暗色包有物」, 岩石鉱物鉱床学会誌
- 4) 大島幹音ほか(2016), 「広島市近郊に分布する広島花崗岩類の形成プロセスの解明」 環境研究論文集 11, 広島大学附属高等学校
- 5) 渡村隆(1989), 日曜の地学 7 広島県の地質をめぐって 増補版, 学芸書院

Where does a dropped coin go?

Hiroshima University High School
TAKASHIMA Akihiro, SASAKI Kokoro, SUGIYAMA Hironobu

Abstract

We have been studying about where a dropped coin goes. The method was that we changed the situation how to drop a coin, and then we dropped a coin 400 times in each situation and took data. We found two things. One is that a dropped coin is more likely to go in the direction which is vertical to the face of a coin. The other is that when we drop a coin from a vertical position, it is more likely to stop at two points, but when we drop it from a horizontal position, the result varied as the height changed.

Motive

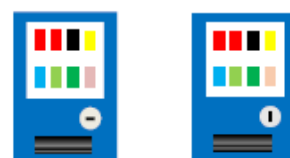


Fig.1 Two types of vending machine

Purpose

- find where a dropped coin is more likely to stop

Method

1. Draw a large ellipse
2. Move shrunk ellipse on the x-y plane
3. Find the central point of the ellipse in which it has the most number of points
4. Change the area of ellipse and repeat 2 and 3

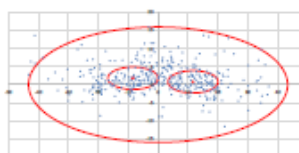


Fig.2 From a vertical position, 0.5 m

Result

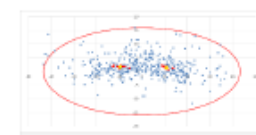


Fig.3-1 From a vertical position, 0.5 m



Fig.3-2 From a vertical position, 1.0 m

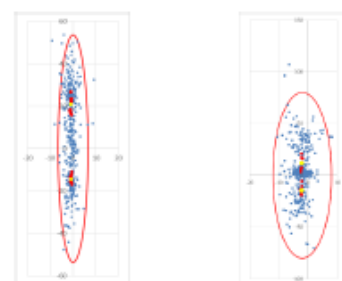


Fig.4-1 From a horizontal position, 0.5 m

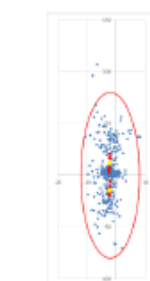


Fig.4-2 From a horizontal position, 1.0 m

Consideration

- form an ellipse
- vertical → two points
- horizontal → vary with height

Prospect

- quantify
- horizontal → the relationship between the number of rotations and the height

Mathematical Analysis of Novels

Hiroshima University High School Second Grade Mathematical research team
Chiharu Kagemoto Nana Tanaka Ayano Fukumizu Natsuki Miyake

Motive

We thought that more novels which are easy to read are written recently than early 20th century. Then in this study we will research about characteristics of easy-to-read novels by some mathematical approaches.

Objects of Analysis

	Title	Author	Genre
Recent Novels	① WAKU WAKU	Yasunari Kawabata	Third person
	② THE RAIN	Yasunari Kawabata	First person
	③ THE RAIN	Yasunari Kawabata	First person
Modern Novels	④ KUMA NO SHIKIISHI	Yoshiko Kuroki	Third person
	⑤ THE RAIN	Yasunari Kawabata	First person

Heads

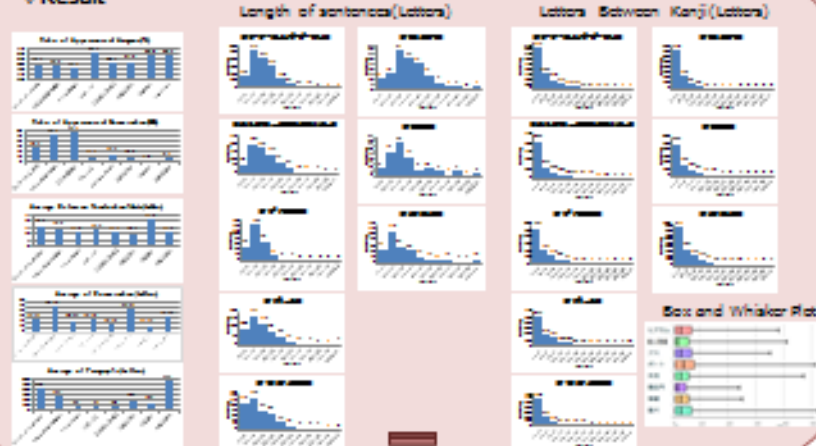
- Ratio of Appearance of Hiragana
- Ratio of Appearance of Conversation
- Average Between Punctuation Marks
- Average Letters of Conversation
- Average Letters of Paragraph
- Length of Sentences
- Letters Between Kanji

How to Analysis

- Digitize these novels
- Count with seven points above
- Make some questionnaires by the conclusion of counting
- Count the answers of questionnaires and analyze the conclusion by each points

In reality, which is "easier to read", recently novels or early 20th century's novels?

Result



Consideration

- Ratio of Appearance of Hiragana
 - Recent in third person novels
 - In first person novels, there are more Hiragana letters of conversation
 - Ratio of Appearance of Conversation
 - Recent in third person novels
 - In first person novels, there are conversation and other characters with lots of marks
 - Larger in recently novels
 - There are many variations in recently novels
 - Average Between Punctuation Marks
 - More variation in recently novels
 - In these days, authors talk individually
- Standard Deviation
 - Recent Novels 1.77 Modern Novels 0.99

- Average Letters of Conversation
 - There are no differences between recently and early 20th century's
 - Average of first person novels - 30 letters
 - Average of second person novels - 30 letters
 - Average Letters of Paragraph
 - More gaps between the main and the branch
 - Average of recently novels - 100 letters
 - Average of early 20th century - 100 letters
 - Length of Paragraph
 - Average 20th century novels, there are many sentences with more than 30 letters
 - Ratio of Letters between Kanji
 - Letters Between Kanji
 - There are almost no differences
 - No differences between age or person

On Questionnaires

The main questionnaires based on these results, and analyzed investigation on 24 grade students of Hiroshima University junior high school and 30 grade students of Hiroshima University high school.
Data sheet is on the presentation

Prospect

Observe the investigation method of "Average of Paragraph" and realize "Paragraph" character questionnaires. Copy the method to other of Japanese and English novels

Analysis of Novels Using Statistics

Hiroshima University High School Second Grade Mathematical research team
Chiharu Kagemoto Nana Tanaka Ayano Fukumizu Natsuki Miyake

Motive

Akutagawa Ryunosuke Prize and Naoki Sanjugo Prize are ones of the most famous novel prizes in Japan.

It is said there are some differences between these, but those differences are so ambiguous that there have been some discussion about them.

We will examine novels which won these prizes to define the characteristics through mathematical approaches.

Hypothesis

- Ratio of appearance of hiragana
Akutagawa's standard deviation > Naoki's
- Ratio of appearance of conversation
Naoki's average > Akutagawa's
- Average between punctuation marks
It reflects author's characteristics clearly
- Average letters of conversation
Naoki's average > Akutagawa's
- Length of sentences
Naoki's average > Akutagawa's
- Average letters between kanji
Akutagawa's standard deviation > Naoki's
- Amount of blanks per page
Akutagawa's standard deviation > Naoki's

Objects of Analysis

	Title	Author	Winning Year
Akutagawa Prize	① WAKU WAKU	Kazuo Otsuki	1937
	② Shinobu	Tetsuro Mura	1960
	③ Sotomaru	Natsuki Miyake	1967
	④ Kuma no shikishi	Yoshiko Kuroki	2000
Naoki Prize	⑤ Shinobu	Tetsuro Mura	1960
	⑥ Sotomaru	Natsuki Miyake	1967
	⑦ Soul Music Lovers Only	Emi Yamada	1967
	⑧ No ten no gogatsu	Yoshi Funado	2000

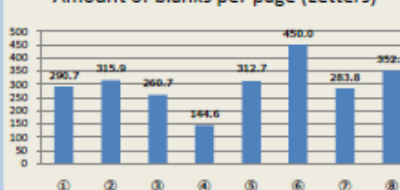
We use about 20,000 letters from each books.
※If the books originally have less than 20,000 letters, we use the whole text.

Consideration

- Ratio of appearance of conversation
Naoki's standard deviation > Akutagawa's
- Average between punctuation marks
Akutagawa's average > the other
& Akutagawa's standard deviation

※Data of ⑥ [Sakuran] are excluded because they are outlier.

Amount of blanks per page (Letters)



- Length of sentences
Akutagawa's average > Naoki's
Naoki's standard deviation > Akutagawa's
※Data of ④ [Kuma no shikishi] are excluded because they are outlier.
- Average letters between kanji
Average & standard deviation
→No differences (≠the other)
Average of largest number & standard deviation of largest number

→Akutagawa's > Naoki's
= Akutagawa's books tend to use hiragana, not kanji for nouns and adjectives
Amount of blanks per page
Naoki's average > Akutagawa's
Akutagawa's standard deviation > Naoki's
= Naoki's books have shorter paragraph.

Conclusion

Six items are characterized by the differences of each prize: ratio of appearance of hiragana, Ratio of appearance of conversation, average between punctuation marks, length of sentences, average letters between kanji, and amount of blanks per page.

Akutagawa Prize

Tend not to use period; longer sentences; Tend to use Hiragana for noun and adjective intentionally

Naoki Prize

Various styles in conversation; shorter paragraphs



For Better Meringue, How to Whip Egg White

**Yuri Amakawa
Tomoka Nogami
Sora Hirokane
Hazuki Miyake
Ryo Yamasaki**

What is Meringue?



Meringue



- **Cake**
- **Cookie**



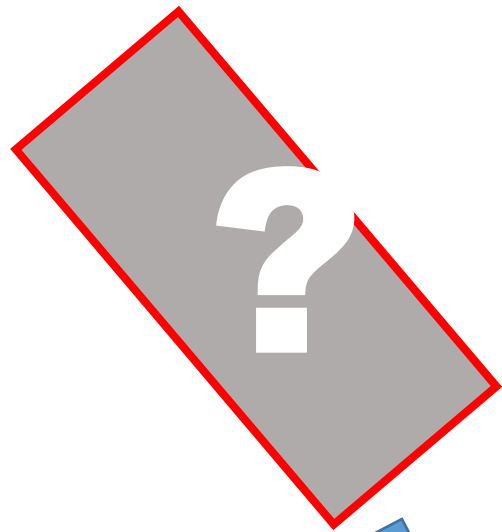
Making good meringue is... **Difficult!**



It takes a long TIME...



It returns to liquid...



1. Salt



2. Sugar



3. Citric acid



4. Soda

If you want to know the answer...

Please come to our poster!!

For Better Meringue, How to Whip an Egg White

Hiroshima University High School Science Club 2nd grade

Yuri Amakawa Tomoka Nogami Sora Hirokane Hazuki Miyake Ryo Yamasaki

Purpose of the Study

- ① To clarify how conditions affect the quality of meringue and the cause of the change
- ② To discover the best way to whip egg white for better meringue

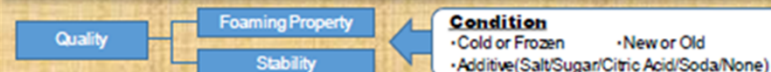


Figure 1 Egg white after whipping

Conclusion

1. Add a little **ACID**, such as citric acid and lemon juice for **well-foaming** meringue
2. Add **NOTHING** for **stable** meringue
3. DO NOT add **ELECTROLYTE** like salt

Pre-Experiment

○Foaming Property

Whip egg white for 90 sec and measure the volume of the meringue.

<Result & Consideration>

- ① The best: Citric acid → Effect caused by pH
- ② Cold > Frozen

○Stability

Measure the amount of liquid separated from meringue 1 hour later.

<Result & Consideration>

Separated Liquid Citric acid > Salt > Soda > Sugar ≈ None
 Little separated liquid = Good Stability
 Stability None ≈ Sugar > Soda > Salt > Citric acid
 → Influence of **Electrolyte**



① pH
 ② Electrolyte
 affect Foaming Property and Stability
 → Advanced experiment on these conditions

Electrolyte = Ion in egg white
 → Measure the amount of ion

Ionic Strength ↑ = Ion ↑



Main Experiment

○Foaming Property

Effect of electrolyte and pH on the density of whipped egg white

pH → Smaller density More salt → Larger density

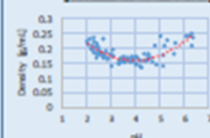


Figure 2 pH and density



Figure 3 Ionic strength and density

○Stability

Measure the amount of liquid separated from meringue 1 hour later

Smaller pH → More liquid More salt → More liquid

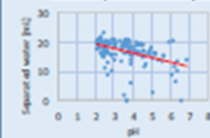


Figure 4 pH and liquid

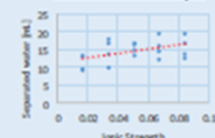


Figure 5 Ionic strength and liquid

Consideration

①Foaming Property

• Ionic Strength ↑ → Foaming Property ↓ (density ↑)
 (Correlation Coefficient...0.39)

• Around **pH** → Foaming Property **MAX**
 ↳ Isoelectric Point of Ovalbumin



②Stability

• Ionic Strength ↑ → Stability ↓
 (Correlation Coefficient...0.47)

• pH ↓ → Stability ↓
 (Correlation Coefficient...-0.61)

Protein attaches with each other → Foaming Property ↑

References

- ・小山静雄, 植田志摩子 「卵白の起泡力および安定度について」, 帯広大谷短期大学紀要28, 63-68, 1991
- ・土井悦四郎 「食品タンパク質の加工特性に関する研究」, 日本食品工業学会誌39(12), 1163-1169, 1992
- ・中村良, 佐藤泰 「鶏卵卵白の泡立ちに関する研究」, 日本農芸化学会誌35(4), 385-390, 1961



数理モデリングの例

金平糖の数理モデリング



広島大学附属高等学校

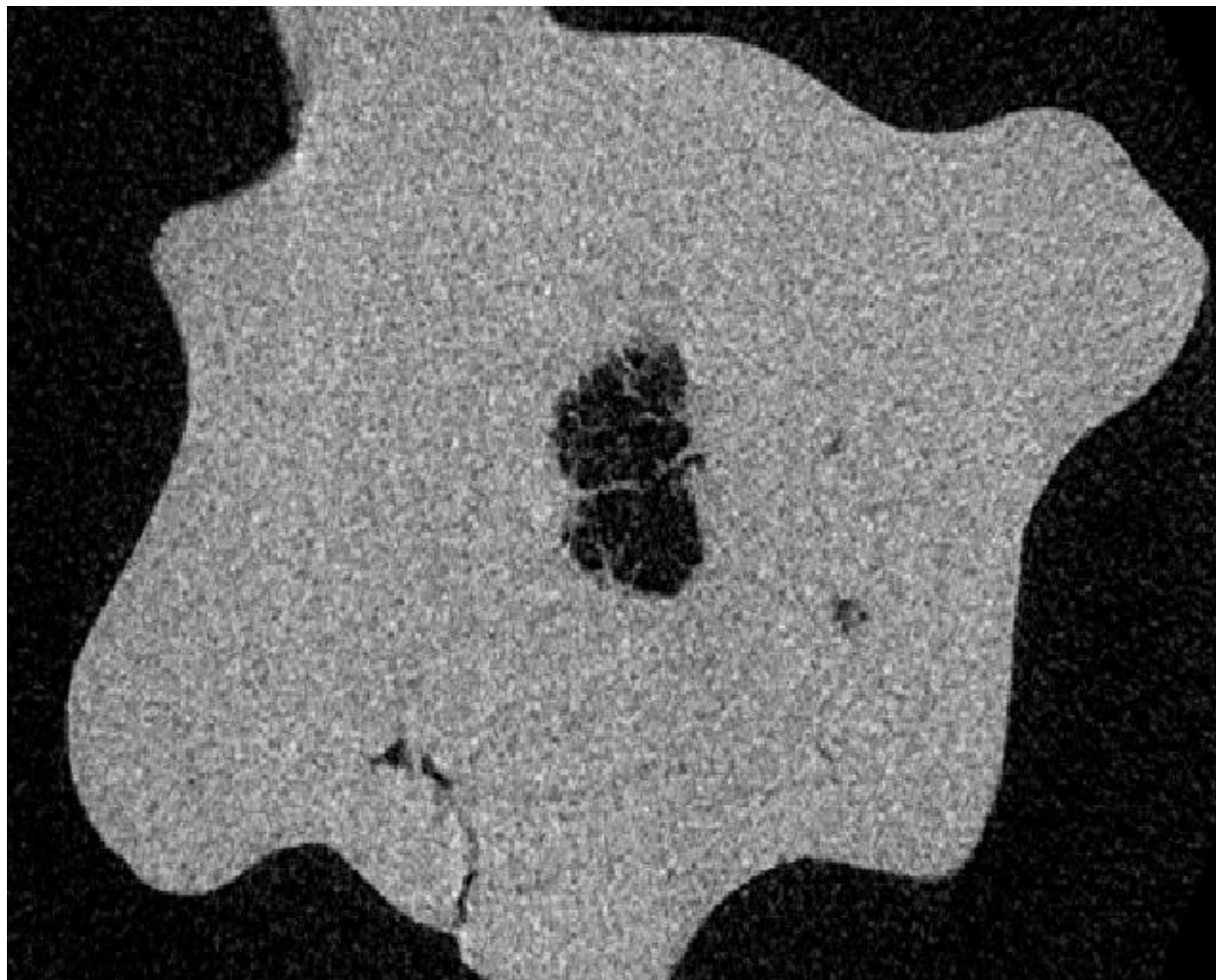
井野口光宏 鈴木蓮 北村晃成
川野達也 小方智景 藤岡真由

金平糖の作り方



(金平糖の作り方 エビス堂製菓)

<http://www.ebisudoseika.co.jp/hpgen/HPB/entries/11.html>より引用)



↑ エックス線CTによる金平糖の断片写真

(宮城新聞 科学ってそもそも何だろう?より引用)

研究目的

- 金平糖の突起部分を角と定め，金平糖が形成されるメカニズムを解明し，それを数理モデルで表す

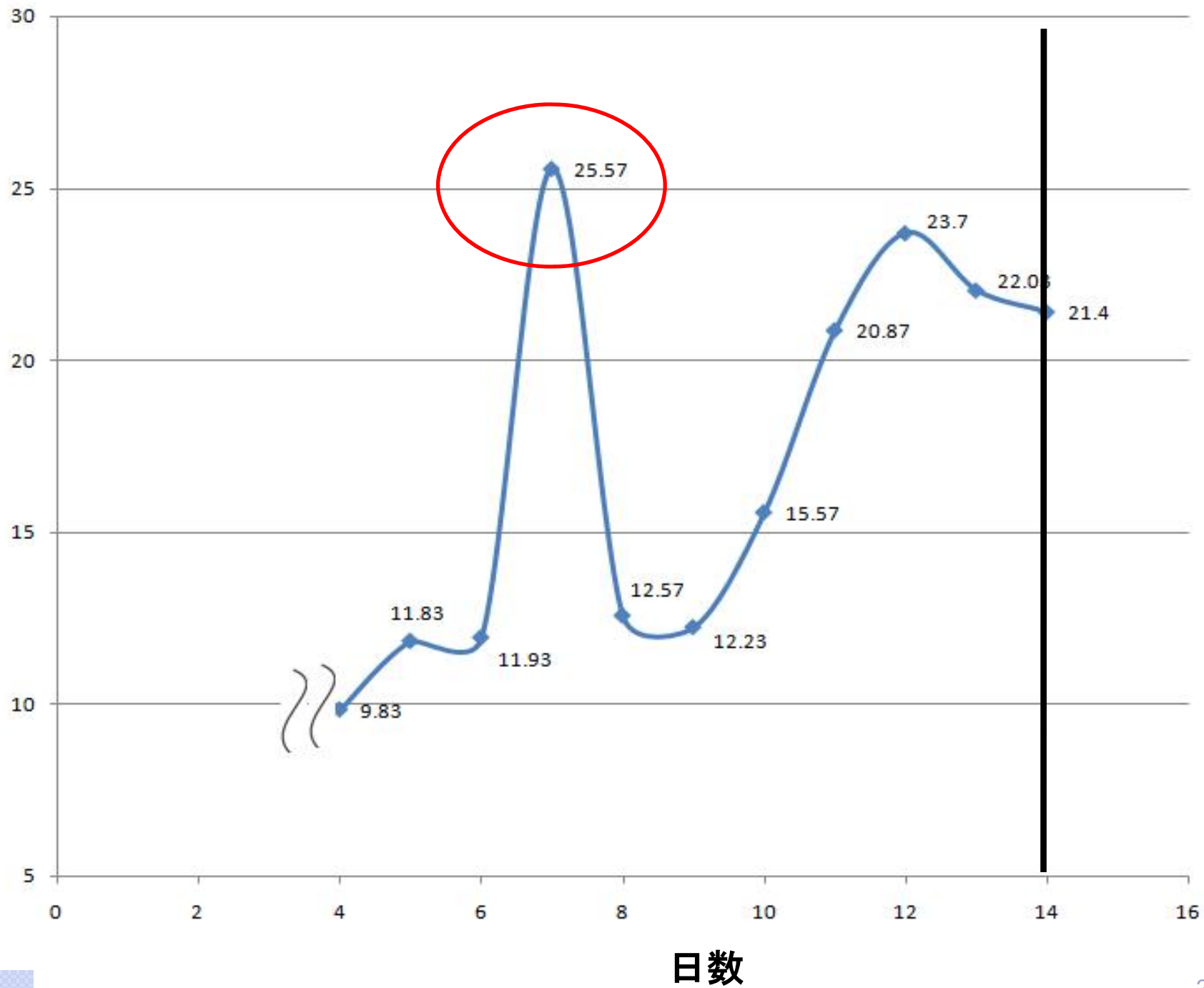
角



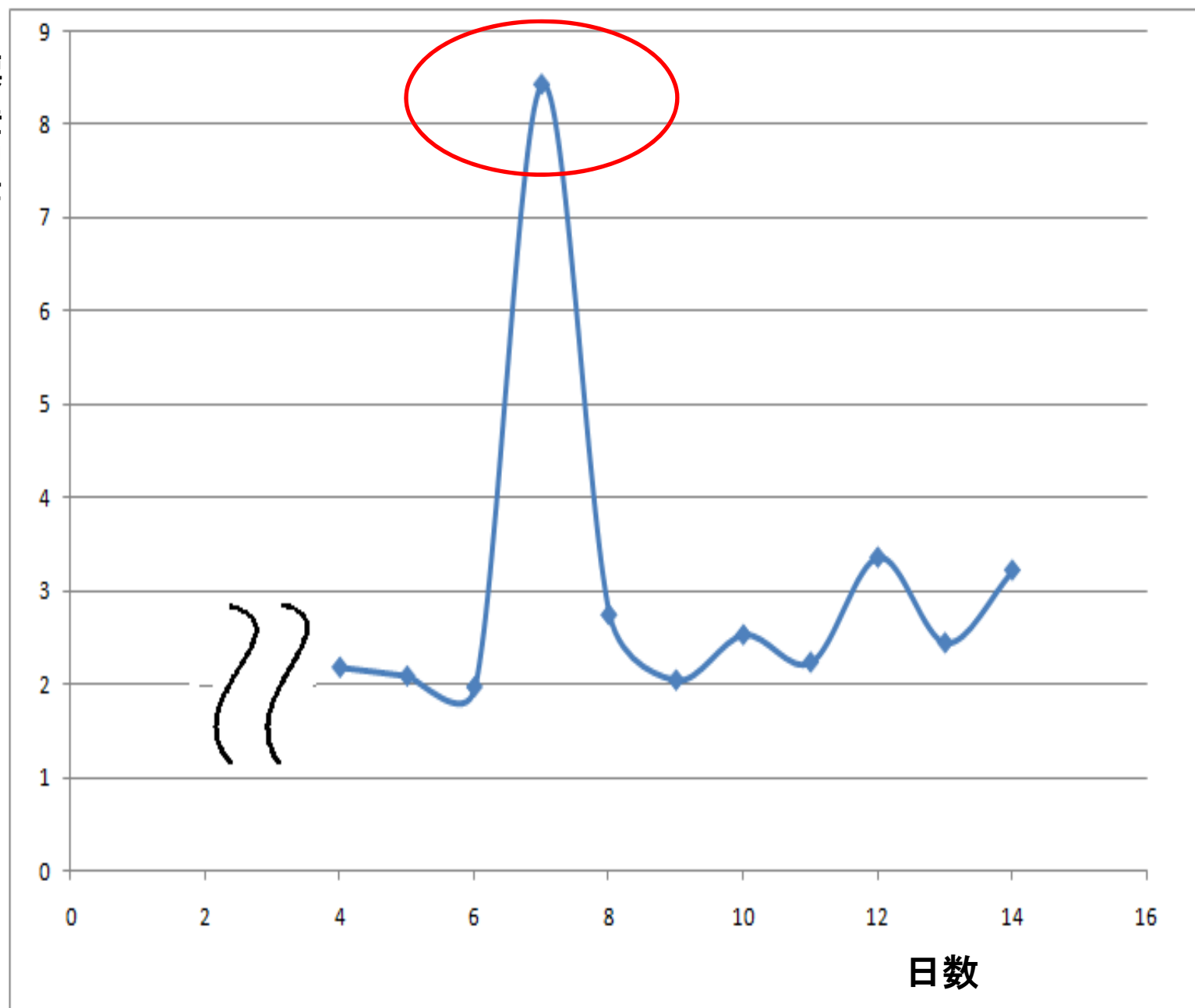
予備実験

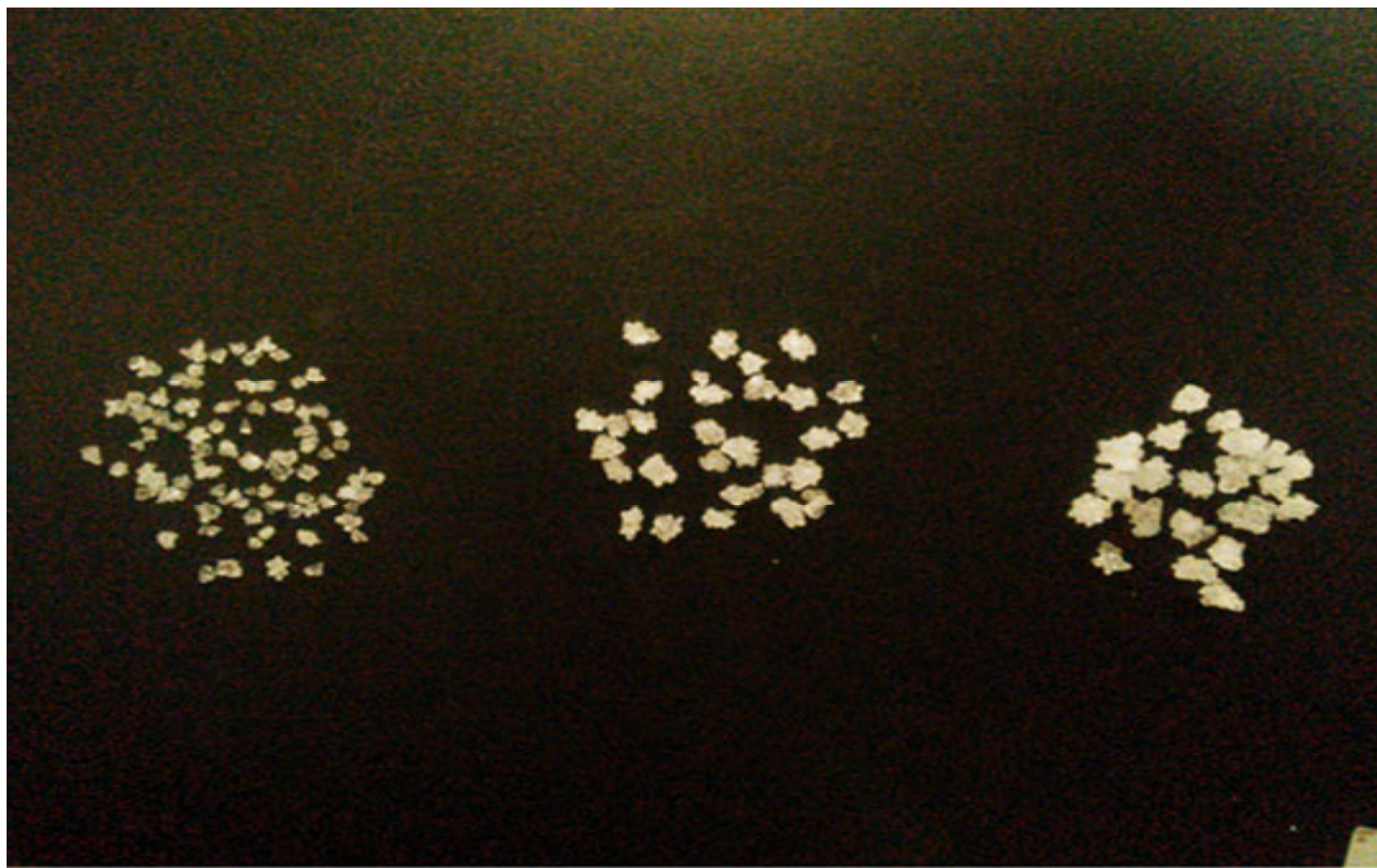
- 1 金平糖を顕微鏡、書画カメラを用いて観察する
- 2 作り始めからの日数ごとに分け、
角の個数を数えて30個の金平糖の
平均値、標準偏差を算出する

金平糖一つ当たりの角の数



標準偏差





(A)

(B)

(C)



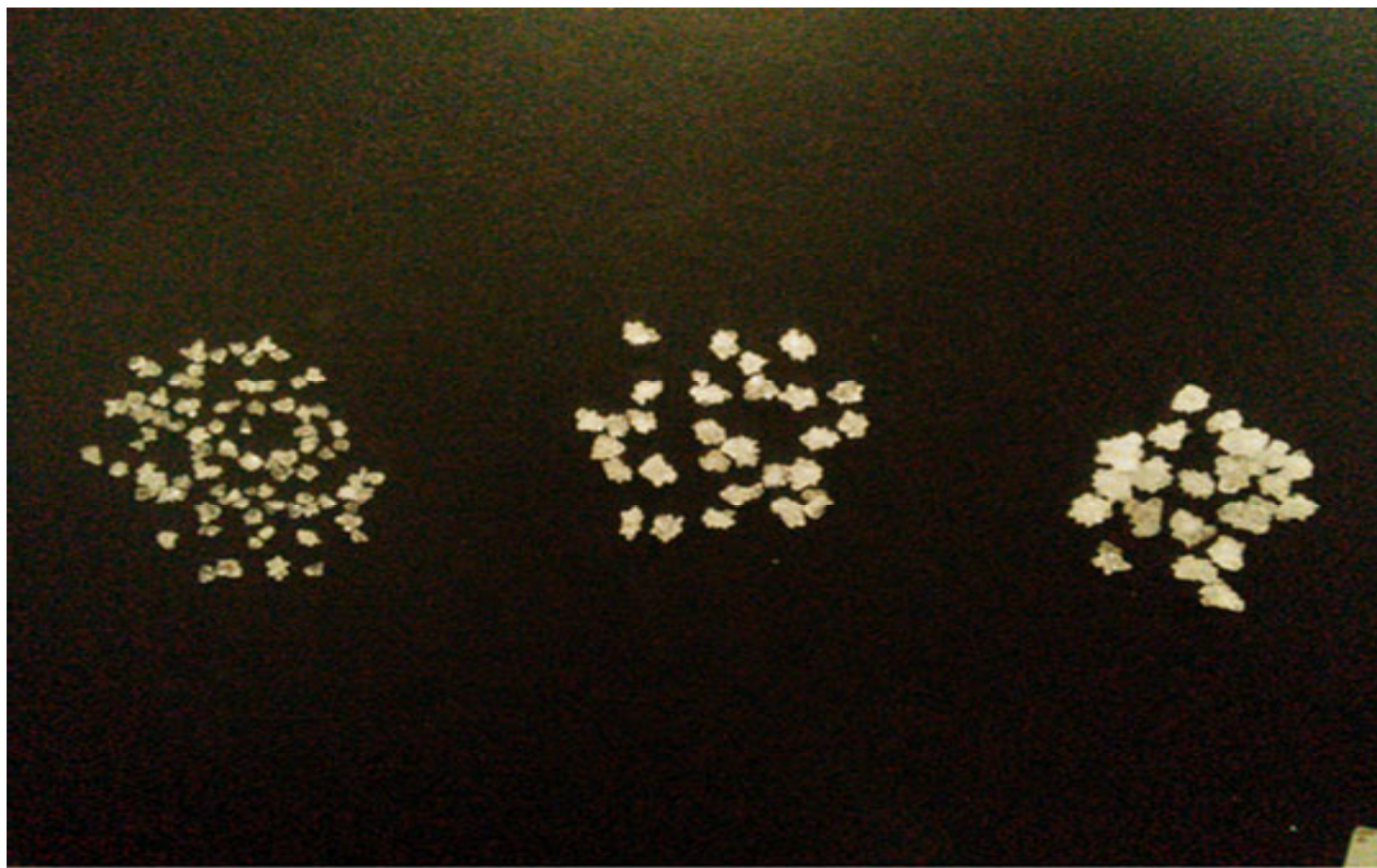
(A)ぶつかってくずれた金平糖



(B) くずれることなく順調に成長した金平糖



(C)ぶつかってくずれた金平糖と結合した金平糖



(A)

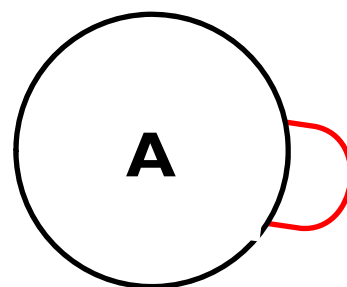
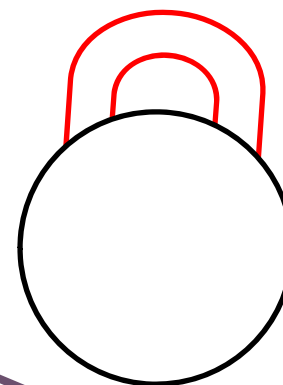
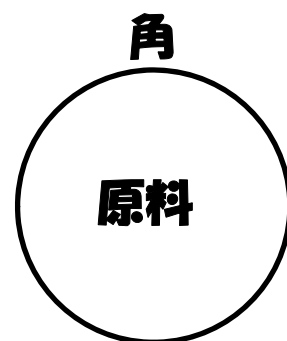
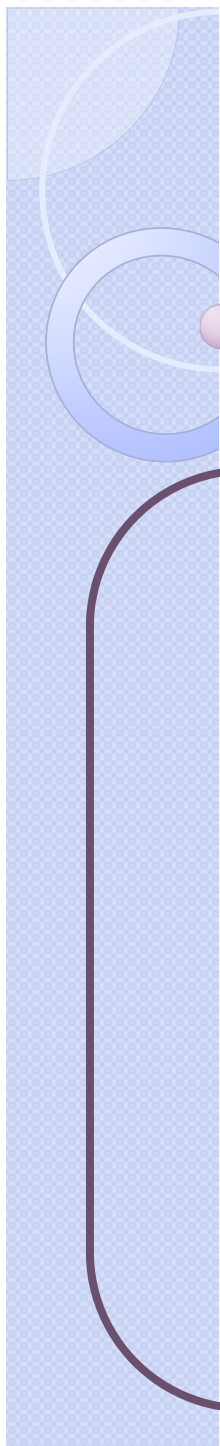
(B)

(C)

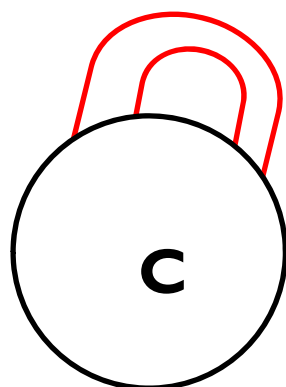
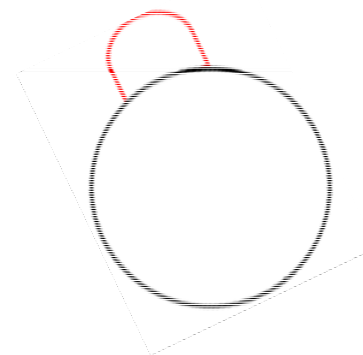
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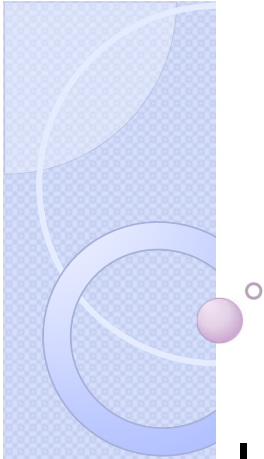
くずれることなく順調に成長した金平糖は、ぶつかってくずれた金平糖とくっつき、小さな角どうしが溶けて結合して大きくなる。

**7,8日目の考察を
ふまえると...**



B





研究内容

- 1 金平糖の角のでき方について確率を用いて
自分たちでルールを定める
- 2 そのルールに従ってExcelで
シミュレーションを行い、
結果をレーダー上にプロットし、
実際の金平糖の断面と比較する

角の形成過程に関する仮説

(早川・酒井, 2007より)

- 突起の高さが高いほど粒子がつきやすい

(予備実験より)

- 隣の地点とある程度の高低差がつくと
角が崩壊する

シミュレーションを行う上での仮定

- 中心となる核、実際の金平糖でいう
ザラメ糖にあたる部分を円と仮定する
- その円の辺をN等分した点上に
結晶化した糖蜜、すなわち突起が付く

シミュレーションに用いた数式

$a_n(t)$: 時刻 t 、地点 n における重なった突起の高さ

$$P_n(t) = \frac{a_n(t)}{\sum_{i=1}^n a_i(t)} \times k$$

$$a_n(t+1) = \begin{cases} a_n(t)+1 & (P_n(t) > Q_n(t)) \\ a_n(t) & (P_n(t) \leq Q_n(t)) \end{cases}$$

$Q_n(t)$: 0～1までを0.01刻みでランダムに
1つ発生させた数

A

時刻t \ 地点N		A	B	C
t-1		12	16	13
t				
t+1				



t-1のときすべての地点についての粒子の合計が648
個だとすると

突起の高さが高いほど新たな粒子がつきやすい
ひとつ前の時間での高さが、粒子のつきやすさに対応する

B

時刻t \ 地点N		A	B	C
t-1				
t		$\frac{12}{648}$	$\frac{16}{648}$	$\frac{13}{648}$
t+1				

B

時刻t \ 地点N		A	B	C
t-1				
t		$\frac{12}{648}$	$\frac{16}{648}$	$\frac{13}{648}$
t+1				



1単位時間に付くと期待できる粒子の数(=k)をかける
 この場合はk=3なので

C

時刻t \ 地点N		A	B	C
t-1				
t		$\frac{12 \times 3}{648}$ 0.055	$\frac{16 \times 3}{648}$ 0.074	$\frac{13 \times 3}{648}$ 0.06
t+1				

C

時刻t \ 地点N		A	B	C
t-1				
t		0.055	0.074	0.06
t+1				

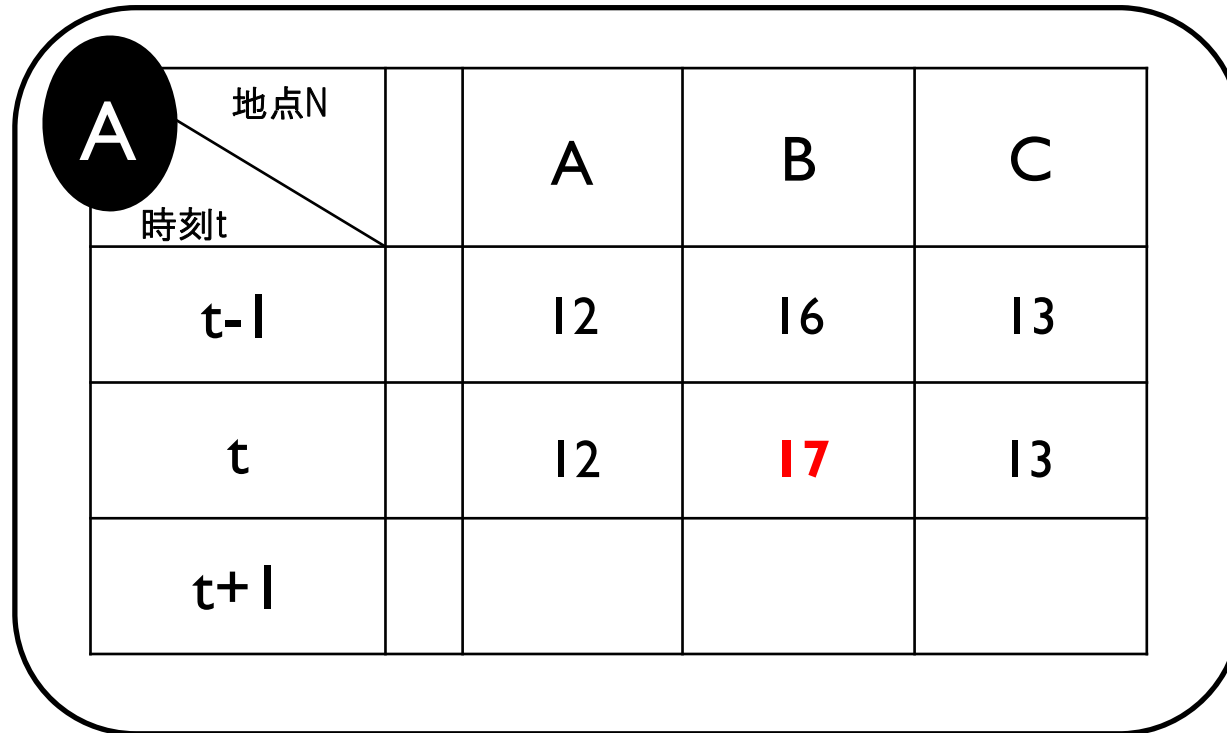
↑ ↑ ↑

この値を比較する！

時刻t \ 地点N		A	B	C
t-1				
t		0.24	0.03	0.54
t+1				

↓ ↓ ↓

0～1を0.01刻みでランダムに発生させた数

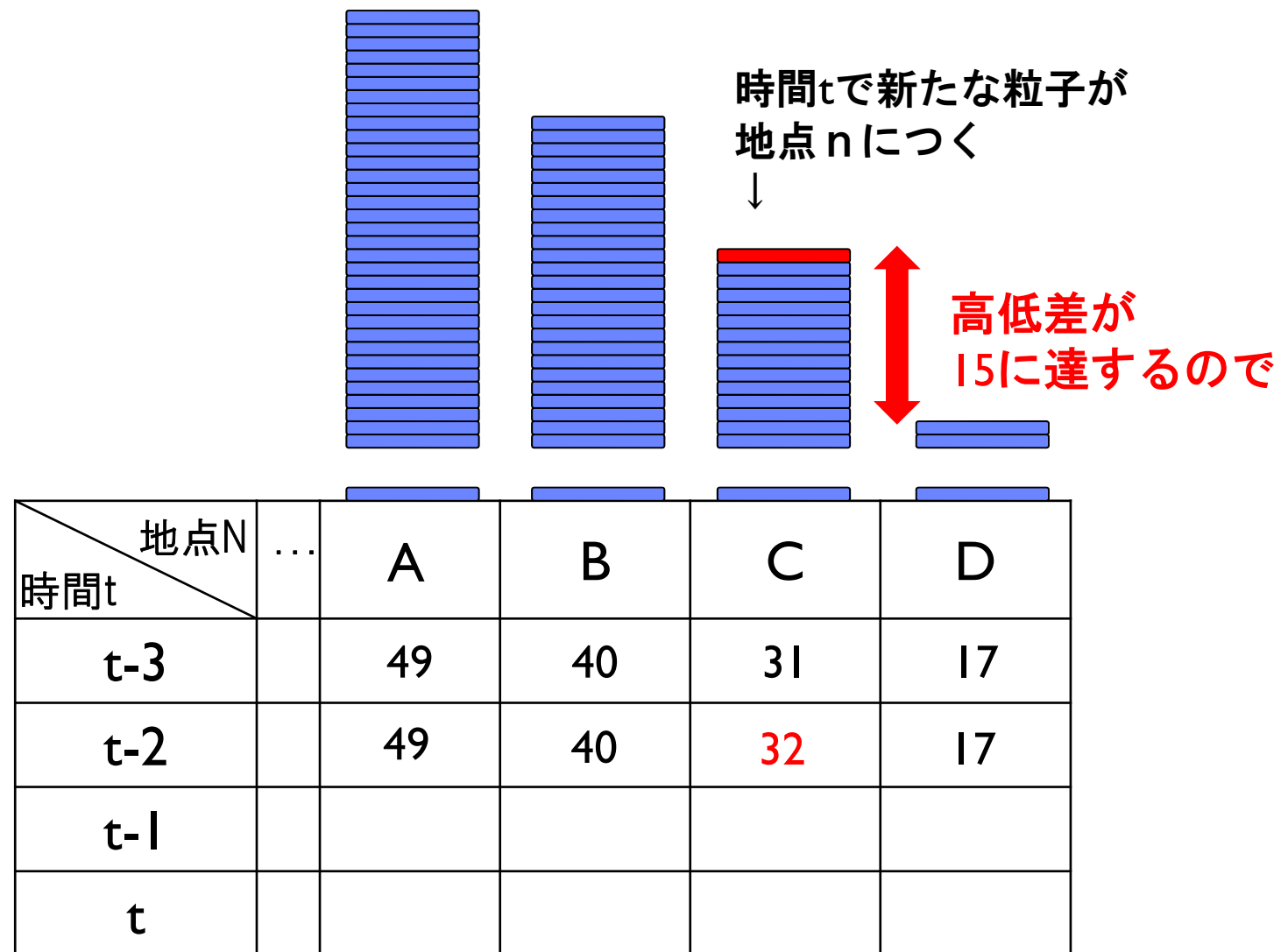


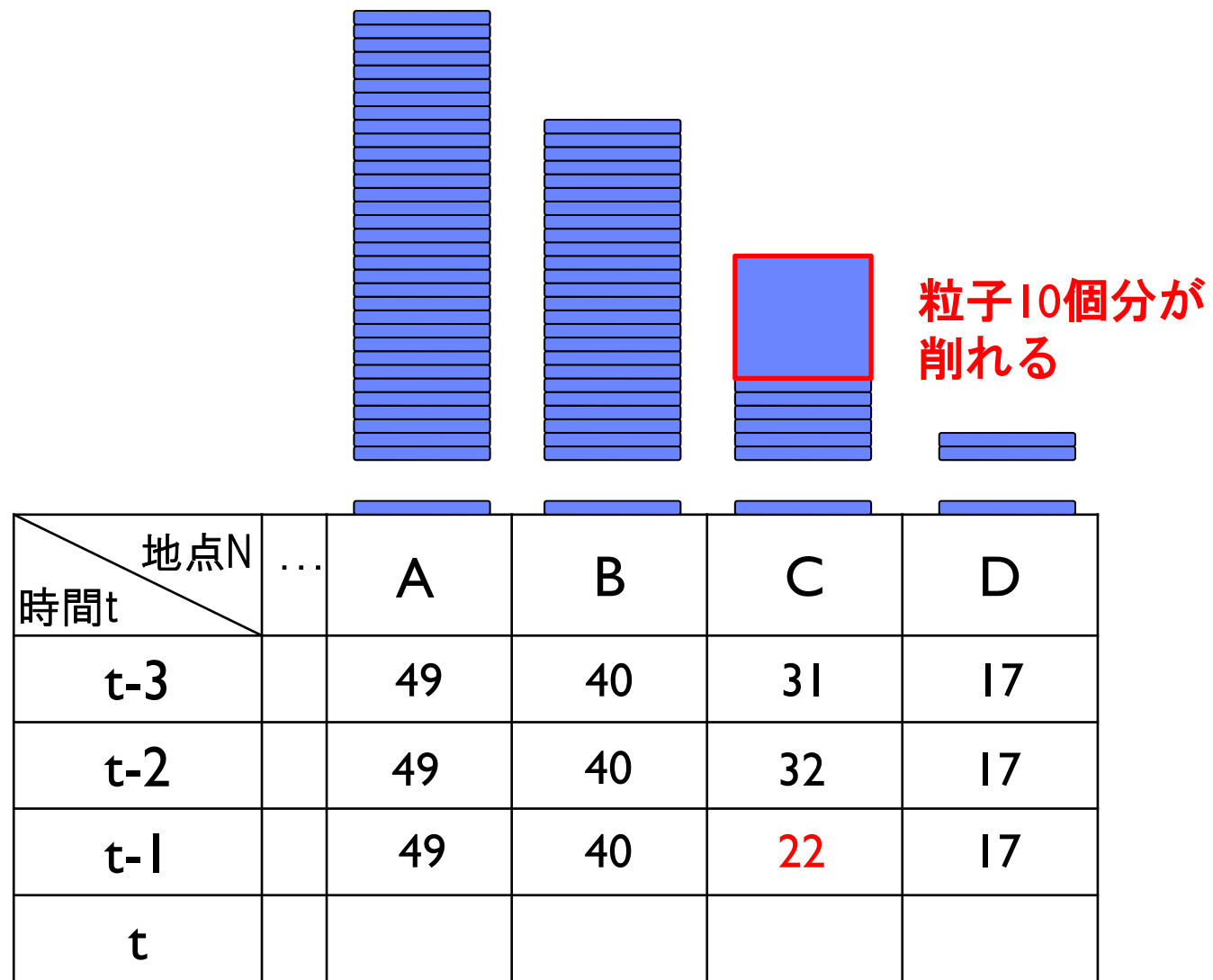
A 時刻t	地点N	A	B	C
t-1		12	16	13
t		12	17	13
t+1				

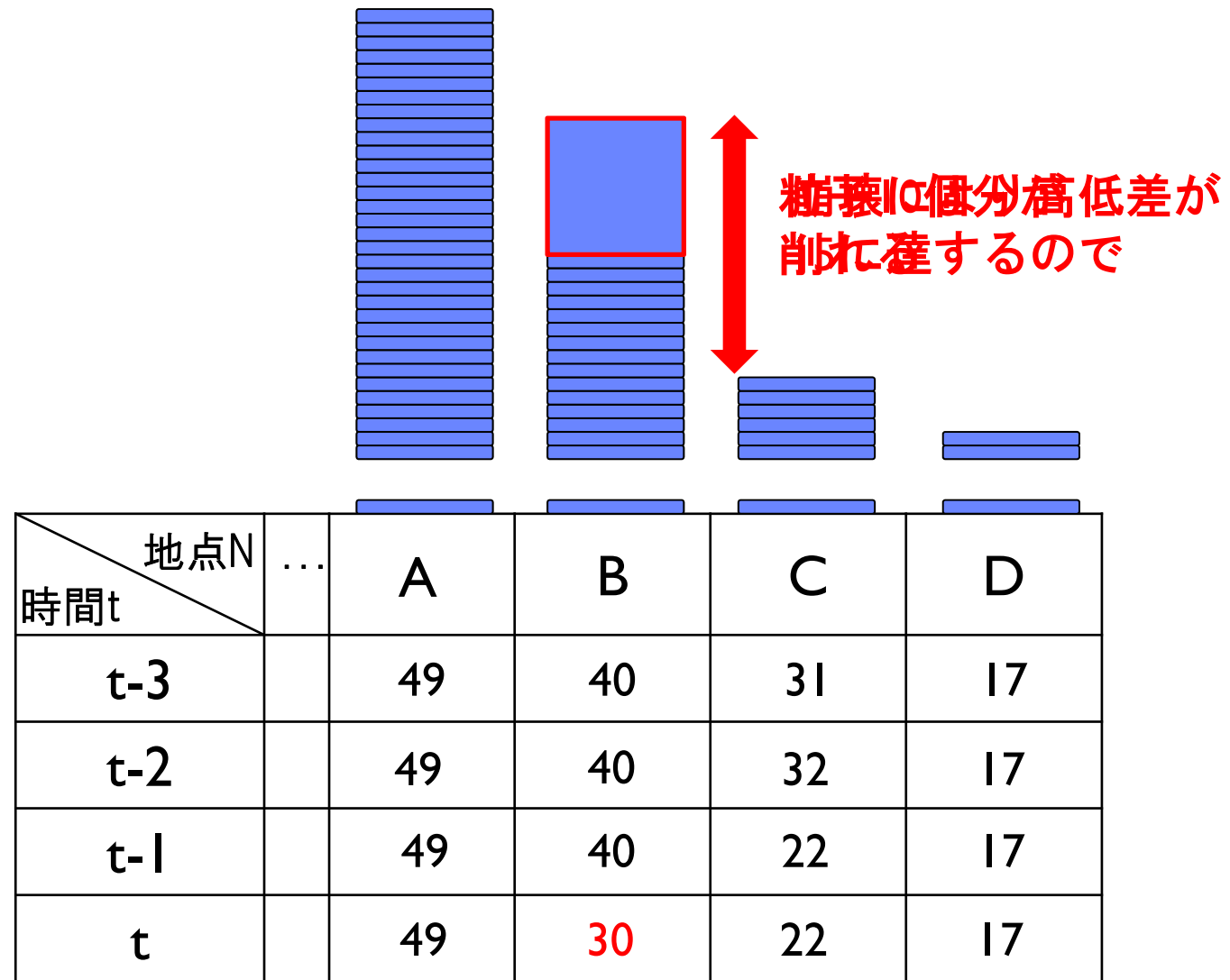
α : 突起が崩壊するときの隣点との高低差=15

β : 一回の崩壊で崩れる高さ=10

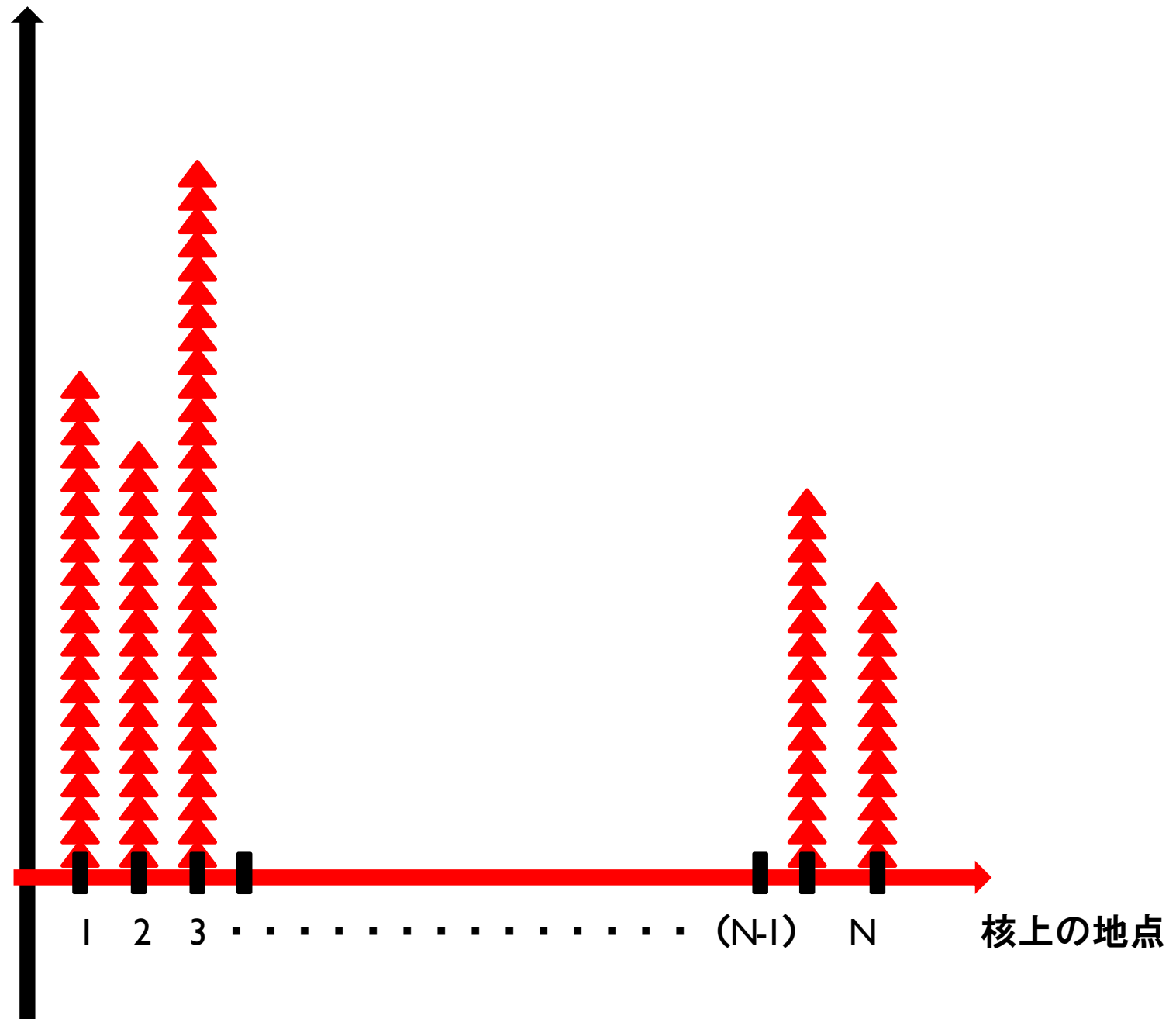
時間t \ 地点N	...	A	B	C	D
t-3		49	40	31	17
t-2					
t-1					
t					



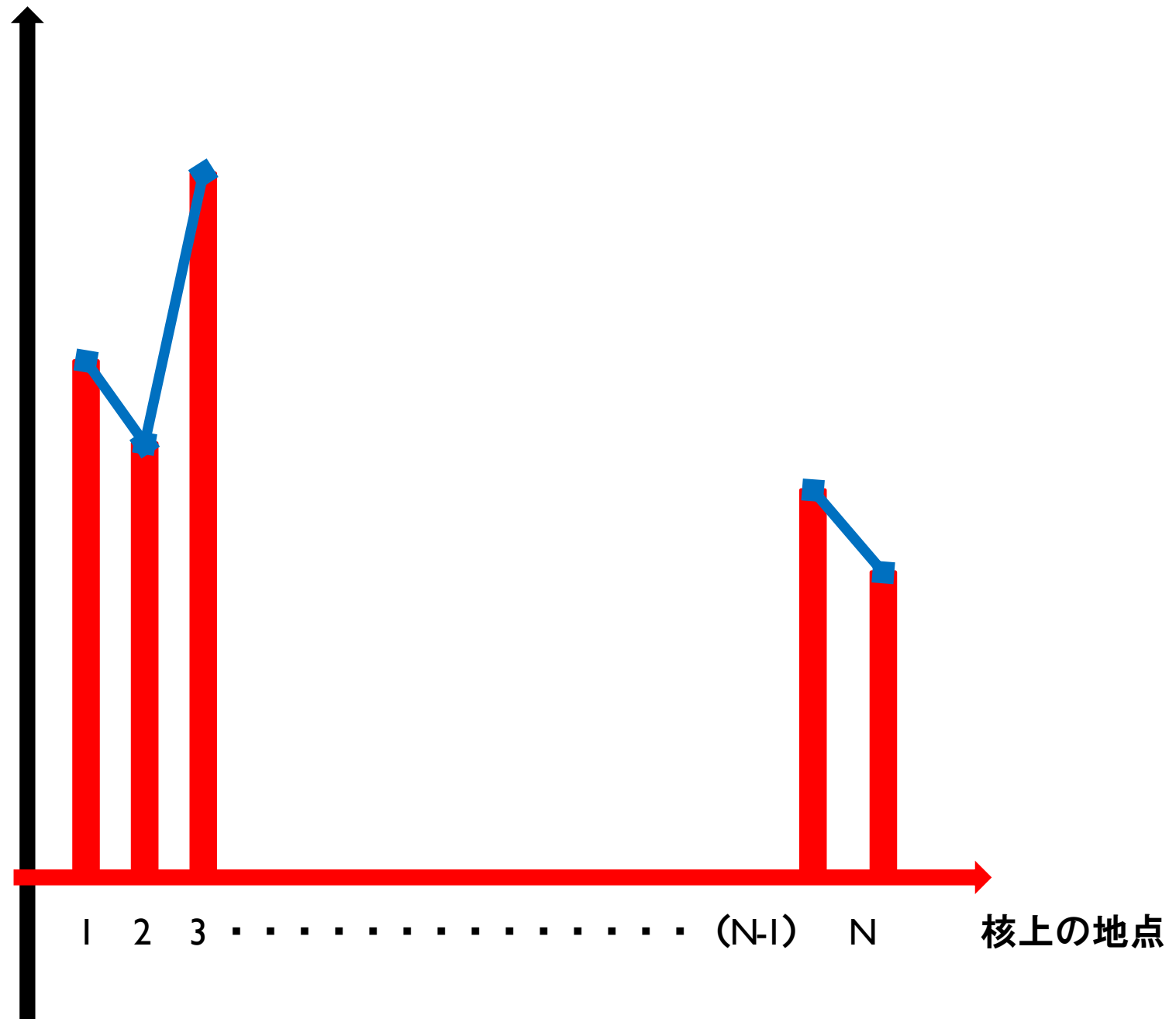


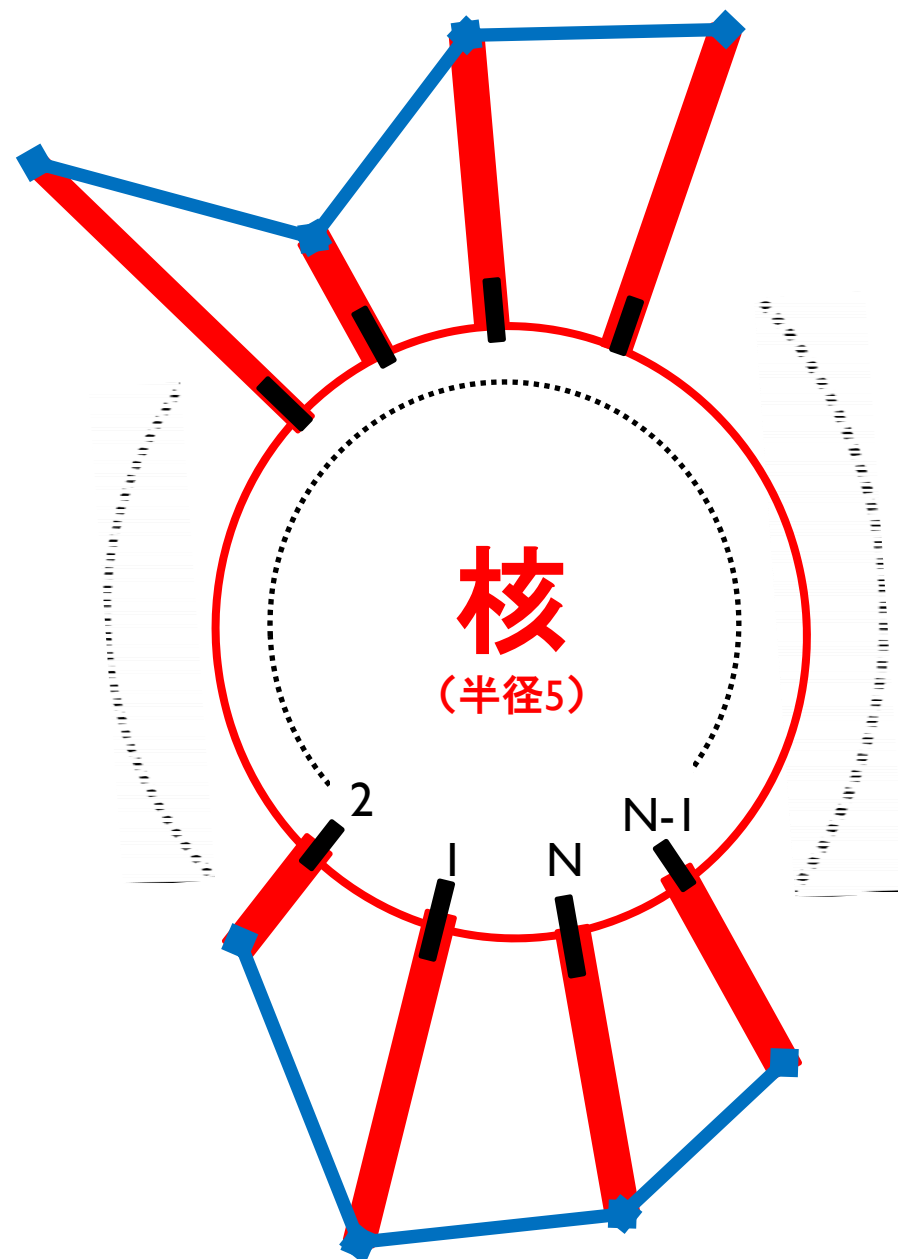


突起の高さ

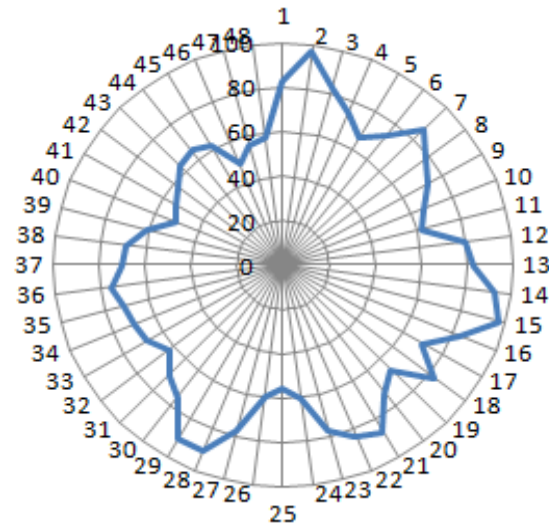


突起の高さ

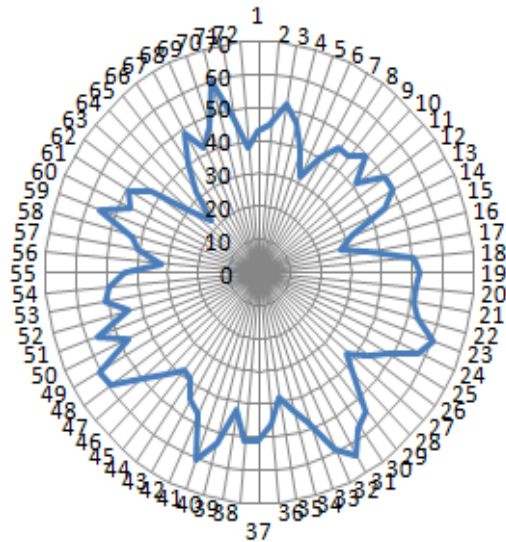




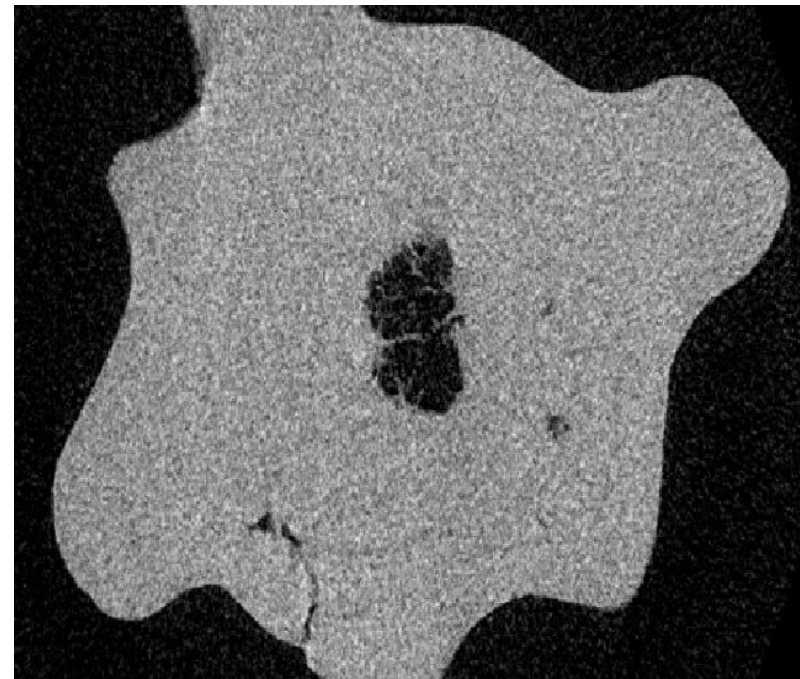
シミュレーションの結果



$\alpha=17$ $\beta=15$ $N=48$ $k=3$



$\alpha=15$ $\beta=10$ $N=72$ $k=3$



今後の課題

以下の方法を用いることでシミュレーションの結果をより現実近づけることができると考えている

- 形が近似している、していないを判断する基準を作る
- 完成する時刻 t の値をより厳密に設定する
- 成長するに従い、単位時間あたりにつく粒子の数が増加する条件を組み込む